

# Modeling Psychological Subgrouping using Multiple Demographic Composition Variables

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May 21, 2013

Modern Modeling Methods Conference

University of Connecticut

# Today's Talk

- Demographic differences in Groups
  - Introduction to the Group Actor Partner Interdependence Model (GAPIM)
- Demographic subgrouping
  - Incorporating multiple demographics with GAPIM
  - Group “Faultlines”
  - Empirical tests of different measurement strategies

# Consequences of Difference in Groups

- **Social Categorization Perspective**
  - Group heterogeneity is negatively associated with **group liking**. (Harrison et al., 1998; Jackson et al., 1993; O'Reilly et al., 1989)
    - **Attraction Paradigm** (Byrne, 1971), **Self-Categorization Theory** (Turner et al., 1987) and **Social Identity Theory** (Tajfel & Turner, 1986)
- **Information/Decision making perspective**
  - Group heterogeneity is positively related to **productivity** (Williams & O'Reilly, 1998)
    - Sommers (2006) found that information was retained more when juries were diverse
    - Evidence is mixed (van Knippenberg, De Dreu & Homan, 2004)

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# Effects of the Others in a Group

- The Attraction Paradigm and Self-Categorization Theory place importance on interpersonal perceptions of similarity
  - First understanding how differences in groups lead to dyadic perceptions of similarity.
- Conceptualizing demographic differences between group members is a complex issue, especially with dyadic outcomes
- Demographics of the *other* group members may affect dyadic perceptions of similarity by potentially highlighting or dampening certain types of difference.

# Conceptualizations of Difference

- Summary measures
  - Mean differences
    - The effect of the group's average, sometimes called group climate (Florin, Giamartino, Kenny, & Wandersman, 1990)

# Traditional Multilevel Modeling (MLM) of Groups

- Variables  $X_{ik}$ , person  $i$ 's gender in group  $k$  (level 1) and  $\bar{X}_{.k}$ , group  $k$ 's mean gender (level 2) to predict  $Y$ .
- Or  $X_{ik} - \bar{X}_{.k}$  (or  $X_{ik}$  “group mean centered”) and  $\bar{X}_{.k}$  to predict  $Y$ .
- Problems with the Traditional MLM Formulation:
  - Part-whole problem.
  - What about other effects of  $X$ , especially diversity in the  $X$ s (or the similarity of the  $X$ s)?

# Conceptualizations of Diversity

- Distance or dispersion measures
  - Sums of multiple proportions
    - Blau's (1977) and Teachman's (1980) indexes
  - Relational Demography
    - The effect of a person's fit into the group or the person's similarity to the other members (Elfenbein & O'Reilly, 2007)

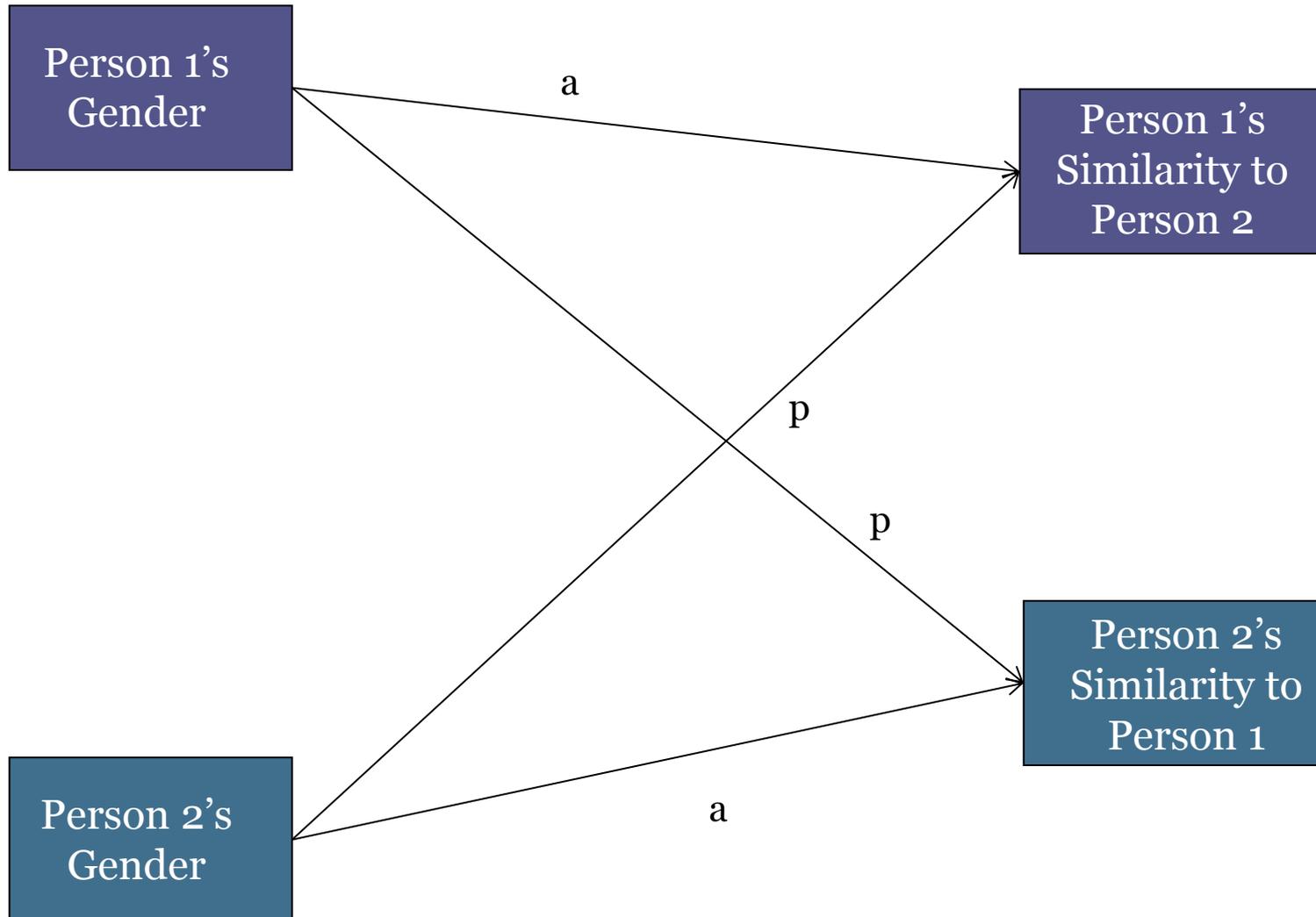
# Conceptualizations of Diversity

- Measuring group diversity
  - Group variance in demographic variable

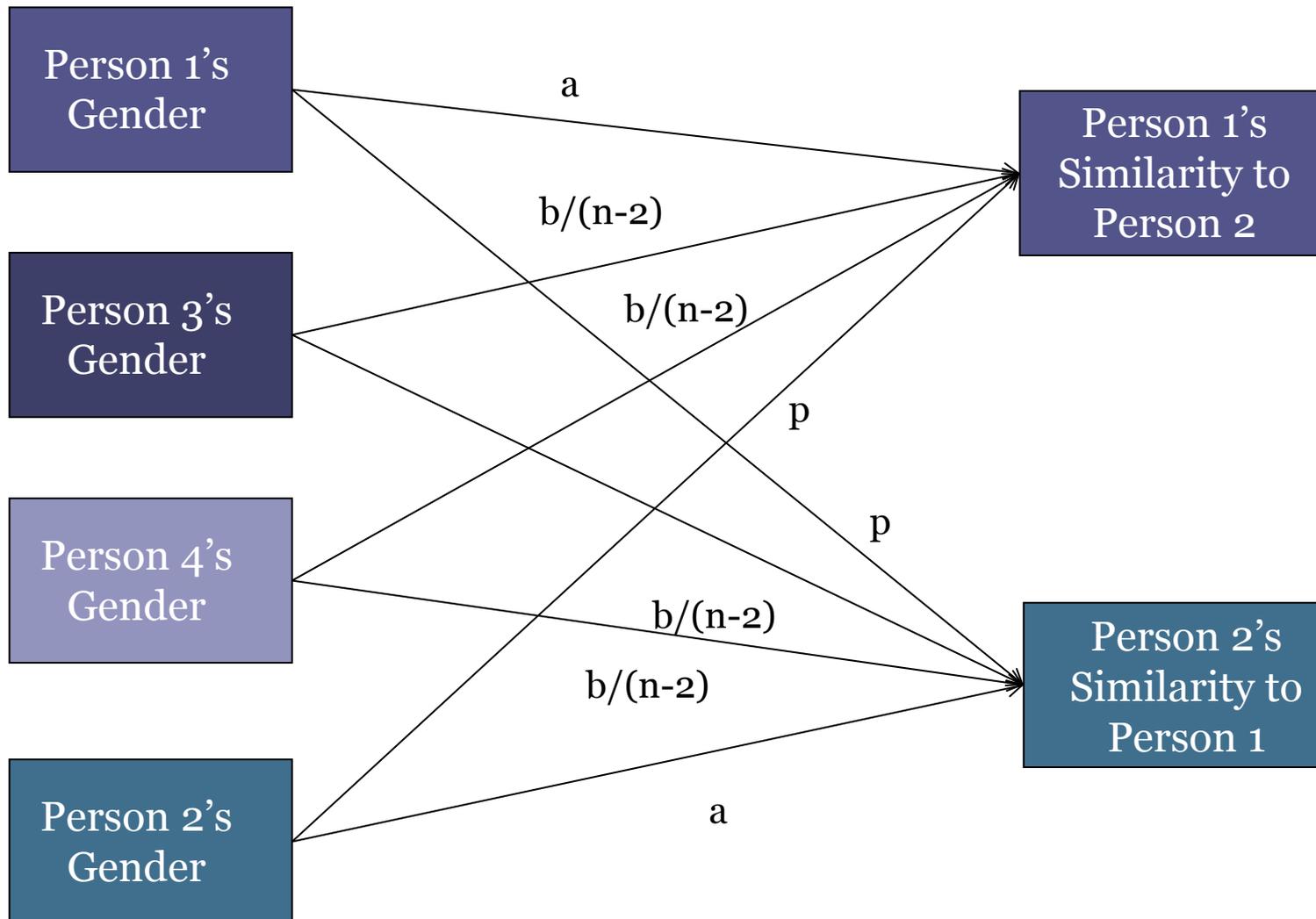
$$S_j^2 = \frac{\sum_{i=1}^n (X_i - \bar{X})^2}{n - 1} = \frac{\sum_{i=1}^{n-1} \sum_{k=i+1}^n (X_i - X_k)^2}{[n(n - 1)]}$$

- where  $n$  is the groups size
- We can decompose *Diversity* depending on the level of measurement of our outcome variable

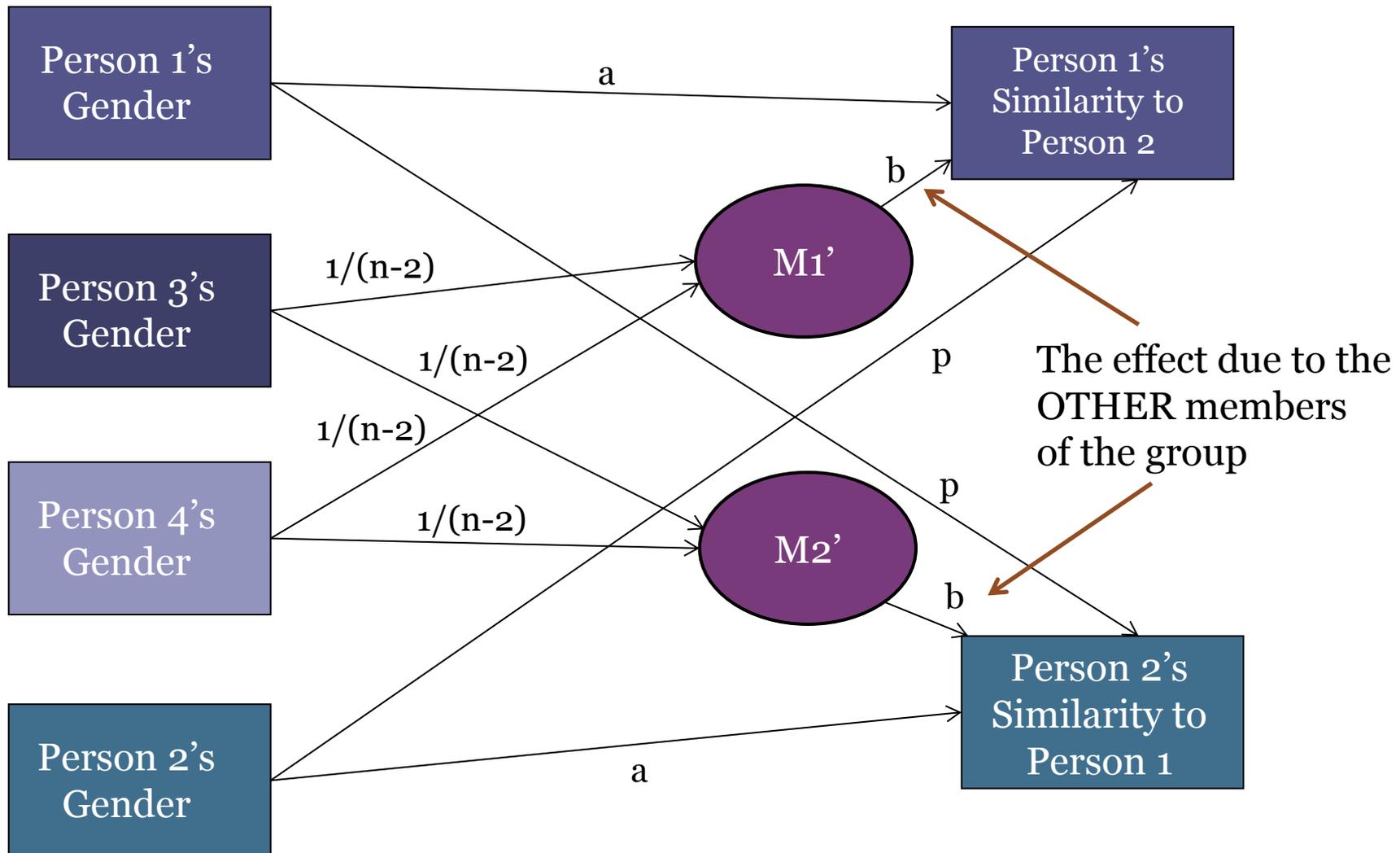
# GAPIM



# GAPIM



# GAPIM



# GAPIM-D

- Mixed Linear Model with 7 fixed effects, 4 random effects, 2 covariances of random effects

$$Y_{ijk} = b_0 + b_1 X_{ik} + b_2 X_{jk} + b_3 X_{ijk}' + b_4 I_{ijk} + b_5 I_{i.k} + b_6 I_{.jk} + b_7 I_{ijk}' + e_{ijk}$$

- $b_1$ : the effect of a person's own gender, the *actor effect*;
- $b_2$ : the effect of the partner's gender, the *partner effect*;
- $b_3$ : the effect of the average gender of the other  $n - 2$  members of the group, the *others effect*;
- $b_4$ : the effect of how similar in gender person  $i$  is to person  $k$ , *dyadic similarity effect*;
- $b_5$ : the average similarity of person  $i$ 's gender to the gender of the other  $n - 2$  members of the group, the *actor similarity*;
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- Plus the Social Relations Model (SRM) random effects to model the nonindependence
  - $\sigma_\mu^2$ : Group variance
  - $\sigma_\alpha^2$ : Actor variance
  - $\sigma_\beta^2$ : Partner variance
  - $\sigma_\gamma^2$ : Relationship variance (error)
  - $\sigma_{\alpha\beta}$ : Generalized reciprocity
  - $\sigma_{\gamma\gamma}$ : Dyadic reciprocity

# Multiple Composition Variables

- People have multiple characteristics that may influence how they categorize themselves and others in small groups. (Brewer, 1995)
- Researchers have recently called for attention to how multiple types of composition variables affect group dynamics simultaneously (Lau & Murnighan, 1998; Lau & Murnighan, 2005; Shaw, 2004; Thatcher, Jehn, & Zanutto, 2003; van Knippenberg, Dawson, West, & Homan, 2011)

# Group Faultline Strength

- “Groups that encompass an identical array of demographic attributes collectively can still have markedly different dynamics if those characteristics are distributed differently among the individuals in a group” (p. 327, Lau & Murnighan, 1998)
- Differences between two group members belonging to different gender groups might be enhanced if these same two group members also belong to different racial groups.

# Faultline Models

- Parallel Interaction Model
  - Interactions of like GAPIM terms across variables
    - Actor race X actor gender
    - Partner race X partner gender
    - Others race X others gender
    - Dyadic similarity race X dyadic similarity gender
    - Actor similarity race X actor similarity gender
    - Partner similarity race X partner similarity gender
    - Others similarity race X others similarity gender

# Faultline Models

- Shaw's (2004) Faultline Strength, FLS
  - Combines a group's internal subgroup alignment...

$$IA_{men.race.obs} = \sum (O_{wi} - E_{wi})^2 / E_{wi},$$

for  $i = 1$  (Black) to  $2$  (White)

- and cross-subgroup alignment...

$$CGAI_{gender} = (N_{fW} \times N_{mW} + N_{fB} \times N_{mB}) / (N_f \times N_m)$$

# Faultline Models

- Shaw's (2004) cont.

$FLS_{gender} = IA_{gender} \times (1 - CGAI_{gender})$ , then

$$FLS = (FLS_{gender} + FLS_{race})/2$$

- When internal alignment is high and cross-subgroup alignment is low this is when  $FLS$  is the highest.
- $FLS_{gender}$  and  $FLS_{race}$  would equal the same value if there were perfect alignment of faultline strength is at its maximum.

# Faultline Models

- Thatcher et al.'s (2003) measure, *Fau*—proportion of variance explained by each split is given by the following equation:

$$Fau_g = \left( \frac{\sum_{j=1}^2 \sum_{k=1}^2 n_k^g (\bar{x}_{.jk} - \bar{x}_{.j.})^2}{\sum_{j=1}^2 \sum_{k=1}^2 \sum_{i=1}^{n_k^g} (\bar{x}_{ijk} - \bar{x}_{.j.})^2} \right), \quad g = 1, 2, \dots, S$$

- where  $n_k^g$  is the number of members in the  $k^{th}$  subgroup on the  $g^{th}$  split.
- $S$  is the number of ways the group can be split into 2 subgroups.
- $x_{ijk}$  is the value of the  $j^{th}$  characteristic for the  $i^{th}$  member of the  $k^{th}$  subgroup
- Denominator is the total variance in race and gender
- Numerator is the variance in race and gender across subgroups.
- Maximum *Fau* is taken as **group's measure** of Faultline strength

# Study 1

Round-robin design

Combined race and gender composition

# Method

- Collected by Culhane, Hosch, and Weaver (2004)
- Gathered from El Paso, Texas jury pool
- 134 6-person juries from the jury pool
  - 54.6% female, 58.5% Hispanic, 31.3% White, 3.9%, Black/African-American, and 2.2% Asian American or Native American.
- Due to missing data in ethnicity 122 groups used in the analyses
- Mock case: Theft
- Jurors rated similarity in a round-robin fashion

## Method (cont.)

- Composition of gender and ethnicity was used
  - Women are coded as -1 and men are coded as 1
  - Hispanic jurors coded as -1 and Non-Hispanic jurors coded as 1

# Group Composition Results

	Gender	Ethnicity
<b>Actor</b>		
<b>Partner</b>		
<b>Others</b>		
<b>Dyadic Similarity</b>		
<b>Actor Similarity</b>		
<b>Partner Similarity</b>		
<b>Others Similarity</b>		

\*  $p < .05$ , \*\*  $p < .01$ , \*\*\*  $p < .001$

# Model Comparisons

<b>Model</b>	<b>SABIC</b>
<b>Additive Model</b>	11111.56
<b>Dyadic Model</b>	<b>11099.68</b>
<b>Parallel Interaction Model</b>	11104.80
<b>FLS Model</b>	11101.63
<b>Fau Model</b>	11101.73

# Summary

- The Dyad Model was the best fitting model
- Some evidence for non-additive effects of race and gender composition.
  - Parallel Interaction Model found an interaction of actor race and actor gender.
- Faultline strength measures did not predict dyadic perceptions of similarity.

# Study 2

Repeated measures design

Manipulated race and gender composition of perceptive groups

# Method

- A total of 156 participants
  - Only those who self-identified as either White/European-American or Black/African-American were included in the analyses (N = 116)
- 20 Black/African American/Caribbean Americans (17.2%), 96 White/European Americans
- 52 men (44.8%) and 64 women
- Ages ranged from 18 to 42

# Method

- Participants are given questionnaires with faces of 4 other “participants” (and their own) who they believe they will soon discuss a topic with
  - The gender (male vs. female) and racial (Black vs. White) compositions of the groups were manipulated.
- Were asked how similar they felt towards each of the other group members.







# GAPIM-D

- Mixed Linear Model with 7 fixed effects, 3 random effects

$$Y_{ijk} = b_0 + b_1 X_{ik} + b_2 X_{jk} + b_3 X_{ijk}' + b_4 I_{ijk} + b_5 I_{i.k} + b_6 I_{.jk} + b_7 I_{ijk}' + e_{ijk}$$

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- Plus random effects
  - $\sigma_\alpha^2$ : Actor variance (random intercept)
  - $\sigma_\beta^2$ : Picture variance
  - $\sigma_\varepsilon^2$ : error

# Group Composition Results

	Gender	Race
<b>Actor</b>		
<b>Partner</b>		
<b>Others</b>		
<b>Dyadic Similarity</b>		
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\*  $p < .05$ , \*\*  $p < .01$ , \*\*\*  $p < .001$

# Model Comparisons

<b>Model</b>	<b>SABIC</b>
<b>Additive Model</b>	1188.72
<b>Dyadic Model</b>	1197.74
<b>Parallel Interaction Model</b>	1190.62
<b>FLS Model</b>	1189.65
<b>Fau Model</b>	<b>1185.94</b>

## Summary of Study 2

- There were dyadic similarity effects for race and gender
- There were effects due to the others—dyadic perceptions of similarity were influenced by the race of the other group members.
- Effects of dyadic similarity in gender and dyadic similarity in race were present in both studies
  - The sizes of these effects varied across studies:  
Study 2 > Study 1

# General Conclusions

- There was some evidence for non-additive effects of race and gender composition, but the specific faultline measures were generally unsuccessful
  - Overlap between the GAPIM parameters and the level of measurement of the outcome variable may be responsible
- Might want to match the Faultline measure to the level of measurement of the outcome.
- Simpler, more intuitive measure of group alignment (correlations) might be better when only two composition variables are involved. With  $>2$  variables more sophisticated methods are needed.

# Thank you!

- Dissertation Advisor
  - David Kenny
  
- Research Assistants
  - Matthew Shang
  - Scott Silvestri
  - AnneMarie Hovasse
  - Brian Albanese
  - Nora Gerardi
  - Amanda Trehern
  - Samantha Rockwood
  - Tyfani Mumford
  - Jennifer Embree
  - Gregory Bruno
  - Erin Huber