

Modeling Cyclical Patterns in Daily College Drinking Data with Many Zeroes

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From simulated to real data...

- ▶ Now we transition from simulation to an applied case where cycles are relevant: College Drinking Data
- ▶ The backdrop: Current approaches to modeling alcohol consumption may be missing rising and falling patterns across days of the week
- ▶ In addition to cycles, drinking data has the added complication of huge stacks of zeroes.
- ▶ This talk will focus on modeling cyclical patterns with a specific type of zero-altered model: a Hurdle model

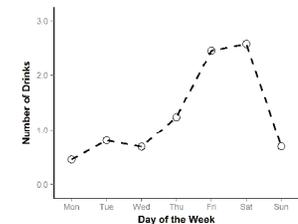
Why do people drink to excess?

- ▶ Let's back up to the big picture. One of the broad questions alcohol researchers care about:
 - ▶ Why do people, including college students, drink to excess?
 - ▶ Important because of the negative consequences^{1,2}:
 - ▶ Greater alcohol-related morbidity and mortality
 - ▶ Greater interpersonal violence
 - ▶ Greater suicide risk
 - ▶ Poorer educational attainment
- ▶ Interest in clarifying factors that predict drinking has driven substance use researchers to pursue intensive longitudinal designs.
 - ▶ e.g., Participants report alcohol use one or more times a day for a set time frame (e.g., 30 days)³.

▶¹Hingson, Heeren, Winter, & Wechsler, 2005; ²Perkins, 2002; ³Kaysen et al., in press

Drinking changes predictably over the week

- ▶ Not surprisingly, daily drinking data shows a predictable pattern over days of the week
 - ▶ Greater drinking on weekends as opposed to weekdays
 - ▶ What is the best way to incorporate this rising and falling rhythm into a statistical model?
- ▶ In the alcohol literature, the most common approach is some type of dummy coding.
 - ▶ Most common is a single dummy variable for weekend vs. weekday.^(e.g.,⁴)
 - ▶ Also seen: dummy codes for individual days of the week^(e.g.⁵)



▶⁴Neighbors et al., 2011; ⁵Simons, Dvorak, Batién, & Wray, 2010

Dummy variables are easy, but problematic

▶ Advantage

- ▶ Dummy variables approaches are simple to implement

▶ Disadvantages

- ▶ Single dummy variable approaches imply an abrupt transition across days of the week.
- ▶ Multiple dummy variables can precisely capture shifts, but are unwieldy, especially with covariates.
- ▶ An attractive alternative is to model data with periodicity as a sinusoidal function

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Saturated time models are unwieldy

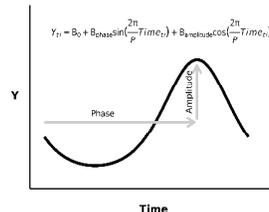
| | Single Dummy | Saturated Dummy | Cyclical terms |
|---------------------------|--|--|--|
| Time Predictor(s) | 1. Weekend vs. weekday | 1. TUE (vs. Monday) 2. WED 3. THU 4. FRI 5. SAT 6. SUN | 1. Amplitude 2. Phase |
| Total | = 1 | = 6 | = 2 |
| With a covariate | 1. Covariate 2. Weekend x Covariate | 1. Covariate 2. TUE x Covariate 3. WED x Covariate 4. THU x Covariate 5. FRI x Covariate 6. SAT x Covariate 7. SUN x Covariate | 1. Covariate 2. Amplitude x Covariate 3. Phase x Covariate |
| Total w/ Covariate | = 3 | = 13 | = 5 |

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Cyclical predictors are straightforward

- ▶ Simple transformation of the linear time predictor (e.g., day of the week) into sine and cosine terms to represent^{6,7}:

- ▶ The magnitude (amplitude)
 - ▶ A location of a regular peak (phase)
1. Multiply the TIME variable by 2π
 2. Divide by the PERIOD ($P = 7$ days)



- ▶ The Amplitude term is the cosine of the above value
- ▶ The Phase term is the sine of the above value

▶ ⁶Fluri & Levri, 1999; ⁷Pinheiro & Bates, 2000

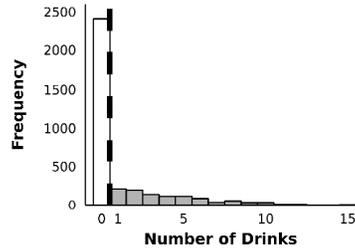
Cyclical Models have a long history

- ▶ Cyclical models of time series data back more than 4 decades
 - ▶ In the biomedical literature, known as “cosinor analysis.”
 - ▶ Early example by Tong (1974) with circadian (i.e., 24 hour) rhythms
 - ▶ Commonly used to model physiological processes.
- ▶ Also adopted within the ecology field
 - ▶ Flury and Levri (1999) examined 24-hour foraging patterns of snails with cyclical logistic regression
- ▶ Pinheiro & Bates’ (2000) classic mixed effects modeling book showed the use cyclical terms in random effects models.
- ▶ To date, rarely used in psychology, but they have attractive features that make them suited for behavioral outcome data.

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Important to attend to excess zeroes...

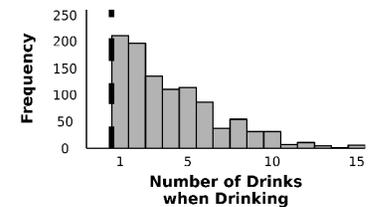
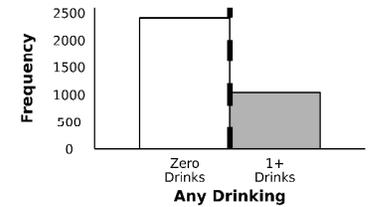
- ▶ Distribution of the data is another important consideration
 - ▶ Behavioral outcomes assessing short intervals will often contain a lot of zeroes.
 - ▶ Substance use
 - ▶ Sexual behavior⁸
- ▶ Zeroes may be a key feature of the phenomena of interest and not just a nuisance of the data.
 - ▶ In the context of alcohol use, the processes that predict...
 - ▶ **the decision to drink at all** may be quite different than
 - ▶ **how much one drinks one they start**



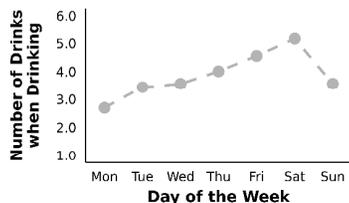
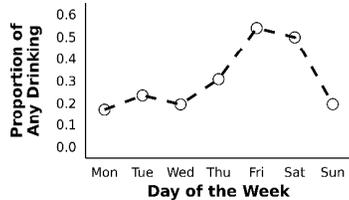
▶ ⁸Bodenmann, Atkins, Schär, & Poffet, 2010

Hurdle models give meaning to zeroes

- ▶ Hurdle models, a type of two-part model are a practical approach
- ▶ A threshold must be crossed from zero into positive counts.
- ▶ As illustrated with the DASH data, the outcome is effectively divided into two parts.
 - ▶ No drinking vs. any drinking:
 - ▶ Logistic regression
 - ▶ Amount of drinking when drinking:
 - ▶ Truncated count regression



Hurdle and cyclical models can be combined



- ▶ Cyclical parameters can be used to model both the binary and positive count models.
- ▶ Can we model trends in any drinking and the amount of drinking when drinking with cyclical models as a sinusoidal function?
- ▶ Plots of mean drinking across days in our recent study of college women suggest cyclical parameters are a reasonable candidate for both.

An example with longitudinal data

- ▶ Project DASH 
 - ▶ Intensive longitudinal study on the association of PTSD and drinking⁹
 - ▶ 172 female undergraduates
 - ▶ Baseline assessment followed by a 30-day monitoring period
 - ▶ On each monitored day, participants completed two PDA assessments

▶ ⁹Kaysen et al., in press

The longitudinal drinking outcome

- ▶ PDA-assessed daily number of standard drinks (**Outcome**)¹⁰
 - ▶ “How many standard drinks have you had in the past 24 hours?”
 - ▶ Participants provided with the definition of a standard drink:
 - **Equivalent to:**
 - 12 oz. can of beer
 - 5 oz. glass of wine
 - 1.5 oz. shot of liquor



▶ ¹⁰Grant, Stewart, O'Connor, Blackwell & Conrad, 1999

A covariate to predict drinking patterns

- ▶ **Self-reported Social Drinking Motives**
 - ▶ Five items from the Drinking Motives Questionnaire-Revised (DMQ-R¹¹)
 - ▶ Example item:
 - ▶ “Because it is what most of my friends do when we get together.”
 - 1 = *never/almost never*
 - 5 = *almost always/always*



▶ ¹¹Grant, Stewart, O'Connor, Blackwell & Conrad, 1999

The regression approach used

- ▶ **Hurdle negative binomial mixed effect regression**
 - ▶ Maximum likelihood estimation
 - ▶ glmmADMB package in R^{12,13}
 - ▶ Two separate regressions:
 - ▶ Binary logistic regression
 - no drinking vs. any drinking
 - ▶ Truncated negative binomial regression
 - number of drinks when drinking
 - ▶ Random effects for each model determined by likelihood ratio tests.

▶ ¹²Skaug, Fournier, Nielsen, Magnusson, & Bolker, 2012; ¹³R Core Team, 2013

Two sets of cyclical vs. dummy variable comparisons

- ▶ **Drinking Trends Only (Models 1-3)**
 - ▶ Baseline models to evaluate the suitability of the cyclical versus dummy variable approaches to modeling drinking data.
- ▶ **Prediction of Drinking Trends (Models 4-6):**
 - ▶ Extend each baseline model with social drinking motives as a moderator of time to assess their performance when evaluating a covariate.
- ▶ **Model's evaluated using BIC and AIC**
 - ▶ BIC's goal is identifying the true model¹⁴
 - ▶ AIC's goal is the prediction of new data¹⁵

▶ ¹⁴O'Connell & McCoach, 2008; ¹⁵Kuha, 2004

A split decision for the cyclical model

| Baseline models | Overall | | Binary | | Count | | Legend |
|--------------------|---------|-----|--------|-----|-------|-----|---|
| | BIC | AIC | BIC | AIC | BIC | AIC | |
| 1. Single dummy | +40 | +78 | +40 | +72 | +49 | +59 | <ul style="list-style-type: none"> Green: "Best" model Blue: second Red: third |
| 2. Cyclical terms | ✓ | +40 | +49 | +75 | ✓ | ✓ | |
| 3. Saturated dummy | +10 | ✓ | ✓ | ✓ | +60 | +50 | |

- Overall, strong evidence per BIC that the cyclical model was the better model of drinking.
 - AIC preferred the saturated model, but cyclical model better predicted the data than a single dummy variable
- However, this obscures differences by sub-model...
 - Cyclical model was a better model for the amount of drinking
 - Saturated model was a better model for the probability of any drinking

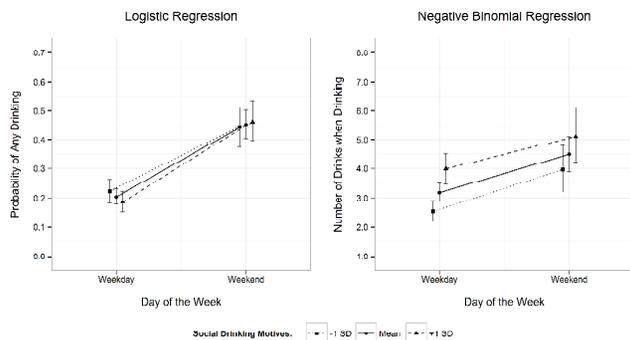


Cyclical and dummy models all evidenced significant moderation

- The next set of models added a covariate (social motives)
 - The weekend, cyclical, and weekday models all detected statistically significant moderation effects in both the probability and amount of drinking
 - Skipping the parameter-by-parameter breakdown, but the complete regression tables are on supplementary slides.
 - The key difference is how informative a picture each model paints about
 - Trends over the week.
 - Differences in those trends by level of social motives



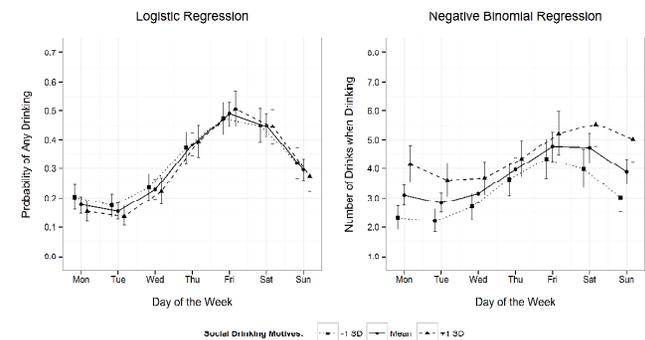
Lack of specificity in weekend moderation models...



- Logistic model:** Greater weekend rise in the probability of any drinking among those with higher social drinking motives.
- Count model:** Smaller weekend rise in the amount of drinking from among those with higher social drinking motives.



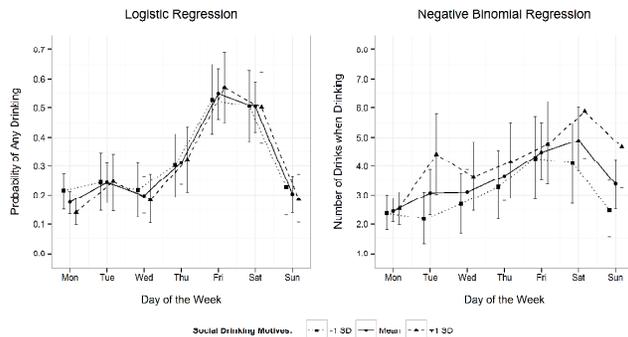
Finer-grained predictions in a cyclical model



- Logistic model:** A more similar probability of any drinking across the week among those with higher motives
- Count model:** Higher and more consistent number of drinks when drinking among those with higher motives



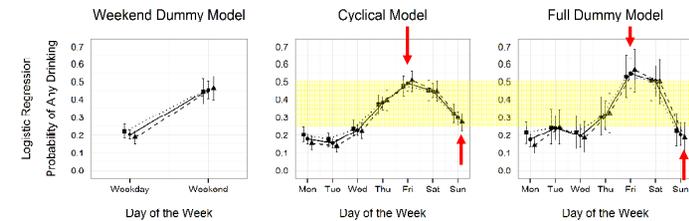
Piecewise predictions in a full dummy model



- ▶ **Logistic model:** Pairwise elevations on Thu and Fri in the probability of drinking compared with Mon among those with higher social motives.
- ▶ **Count model:** Pairwise elevations on Tue and Sun in the number of drinks on compared with Mon among those with higher social motives.

▶

Cyclical model errs in late week prediction of drinking probability



- ▶ **Poorer fit of the cyclical logistic model (seen earlier) coincides with cyclical/full model divergence in late week predictions. Eg.,**
 - ▶ Friday/Saturday predictions about 5% too low
 - ▶ Sunday predictions about 10% too high.

▶

Cyclical regression covariates a qualified success

- ▶ Cyclical regression covariates were a practical alternative to full dummy variables for modeling drinking patterns
 - ▶ More elegant interpretation that focuses on the magnitude of the peak.
 - ▶ Introducing a covariate for time added far fewer parameters in the cyclical model.
 - ▶ More difficult to understand because time divided into many pieces
 - ▶ Unable to estimate random slopes in the saturated model.
- ▶ Cyclical regression parameters were easily combined with hurdle regression
 - ▶ Modeling zeroes versus non-zeroes as a separate process led to richer picture of drinking as a two-part process.

▶

Interesting insights from comparing approaches

- ▶ In particular, not all aspects of drinking were perfectly sinusoidal
 - ▶ The number of drinks when drinking had a rhythmic pattern that was reasonably approximated by cyclical terms.
 - ▶ However, either of the dummy variable approaches were a better model for the probability of any drinking
- ▶ That the very simple weekend model fit better than the cyclical model provides insight into day-to-day differences in the decision to drink.
 - ▶ Suggests there is some homogeneity in the probability of drinking during weekdays, rather than a continuous rise and fall implied by a cyclical model.

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Questions?

- ▶ For post-conference questions, contact:
 - ▶ David Huh (dhuh@uw.edu).

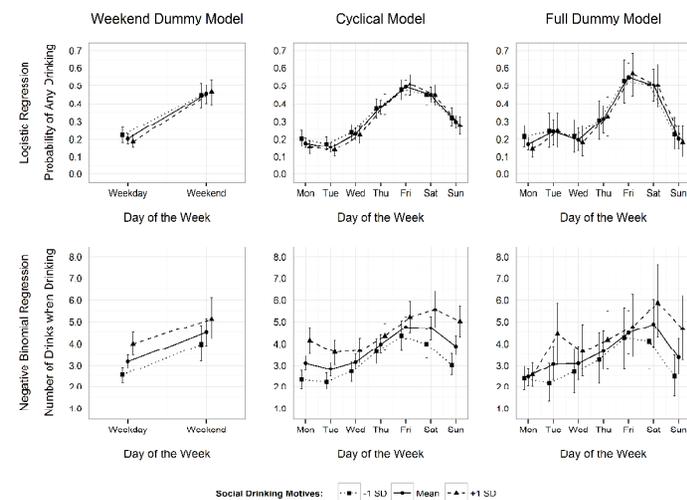
Recommended Reading

- ▶ Example of cyclical models using mixed effect logistic regression:
 - ▶ Bodenmann, G., Atkins, D. C., Schär, M., & Poffet, V. (2010). The association between daily stress and sexual activity. *Journal of Family Psychology*, 24, 271–279. doi:10.1037/a0019365
- ▶ Tutorial on longitudinal count regression methods (including zero-altered models):
 - ▶ Atkins, D. C., Baldwin, S. A., Zheng, C., Gallop, R. J., & Neighbors, C. (2013). A tutorial on count regression and zero-altered count models for longitudinal substance use data. *Psychology of Addictive Behaviors*, 27, 166–177. doi:10.1037/a0029508

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- ▶ Flury, B. D., & Levri, E. P. (1999). Periodic logistic regression. *Ecology*, 80, 2254–2260. doi:10.1890/0012-9658(1999)080[2254:PLR]2.0.CO;2
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- ▶ Kaysen, D. L., Atkins, D. C., Simpson, T. L., Stappenbeck, C. A., Blaynew, J. A., Lee, C. M., & Larimer, M. E. (in press). Proximal relationships between PTSD symptoms and drinking among female college students: Results from a daily monitoring study. *Psychology of Addictive Behaviors*.
- ▶ Kuha, J. (2004). AIC and BIC: Comparisons of assumptions and performance. *Sociological Methods & Research*, 33, 188–229.
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- ▶ Pinheiro, J. C., & Bates, D. M. (1995). Approximations to the Log-Likelihood Function in the Nonlinear Mixed-Effects Model. *Journal of Computational and Graphical Statistics*, 4, 12–35.
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- ▶ Skaug, H., Fournier, D., Nielsen, A., Magnusson, A., & Bolker, B. (2012). glmmADMB: Generalized linear mixed models using AD model builder. *R package version 0.7.3*, 4.
- ▶ Tong, Y. L. (1976). Parameter Estimation in Studying Circadian Rhythms. *Biometrics*, 32, 85–94. doi:10.2307/2529340

Comparing all models simultaneously



Regression Table of Baseline Models

Logistic Regression

| Weekend Dummy Model | B | SE | p |
|---------------------|-------|------|-------|
| Intercept | -1.80 | 0.10 | <.001 |
| Weekend vs. Weekday | 1.38 | 0.09 | <.001 |

| Cyclical Model | B | SE | p |
|--------------------|-------|------|-------|
| Intercept | -1.01 | 0.09 | <.001 |
| Amplitude (cosine) | -0.78 | 0.06 | <.001 |
| Phase (sine) | -0.61 | 0.06 | <.001 |

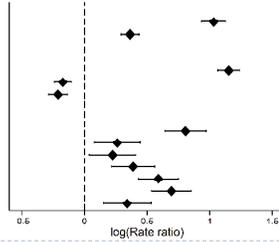
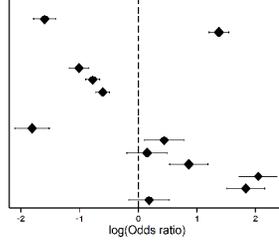
| Full Dummy Model | B | SE | p |
|----------------------|-------|------|-------|
| Intercept | -1.81 | 0.15 | <.001 |
| Tuesday vs. Monday | 0.44 | 0.17 | .01 |
| Wednesday vs. Monday | 0.15 | 0.17 | .40 |
| Thursday vs. Monday | 0.86 | 0.17 | <.001 |
| Friday vs. Monday | 2.04 | 0.16 | <.001 |
| Saturday vs. Monday | 1.83 | 0.17 | <.001 |
| Sunday vs. Monday | 0.18 | 0.18 | .30 |

Truncated Negative Binomial Regression

| Weekend Dummy Model | B | SE | p |
|---------------------|------|------|-------|
| Intercept | 1.03 | 0.05 | <.001 |
| Weekend vs. Weekday | 0.36 | 0.04 | <.001 |

| Cyclical Model | B | SE | p |
|--------------------|-------|------|-------|
| Intercept | 1.15 | 0.04 | <.001 |
| Amplitude (cosine) | -0.17 | 0.04 | <.001 |
| Phase (sine) | -0.21 | 0.04 | <.001 |

| Full Dummy Model | B | SE | p |
|----------------------|------|------|-------|
| Intercept | 0.61 | 0.08 | <.001 |
| Tuesday vs. Monday | 0.26 | 0.09 | .01 |
| Wednesday vs. Monday | 0.22 | 0.10 | .02 |
| Thursday vs. Monday | 0.39 | 0.09 | <.001 |
| Friday vs. Monday | 0.69 | 0.08 | <.001 |
| Saturday vs. Monday | 0.69 | 0.08 | <.001 |
| Sunday vs. Monday | 0.34 | 0.10 | <.001 |



Regression Table of Moderation Models

Logistic Regression

| Weekend Dummy Model | B | SE | p |
|--------------------------|-------|------|-------|
| Intercept | -1.60 | 0.10 | <.001 |
| Social Motives | -0.13 | 0.10 | .16 |
| Weekend vs. Weekday | 1.38 | 0.09 | <.001 |
| Social Motives * Weekend | 0.17 | 0.06 | .04 |

| Cyclical Model | B | SE | p |
|----------------------------|-------|------|-------|
| Intercept | -1.61 | 0.09 | <.001 |
| Social Motives | -0.05 | 0.09 | .52 |
| Amplitude (cosine) | -0.78 | 0.06 | <.001 |
| Phase (sine) | -0.61 | 0.06 | <.001 |
| Social Motives * Amplitude | -0.13 | 0.06 | .03 |
| Social Motives * Phase | -0.02 | 0.06 | .78 |

| Full Dummy Model | B | SE | p |
|----------------------------|-------|------|-------|
| Intercept | -1.63 | 0.10 | <.001 |
| Social Motives | -0.28 | 0.15 | .06 |
| Tuesday vs. Monday | 0.46 | 0.17 | .01 |
| Wednesday vs. Monday | 0.16 | 0.18 | .36 |
| Thursday vs. Monday | 0.86 | 0.17 | <.001 |
| Friday vs. Monday | 2.07 | 0.17 | <.001 |
| Saturday vs. Monday | 1.85 | 0.17 | <.001 |
| Sunday vs. Monday | 0.20 | 0.18 | .26 |
| Social Motives * Tuesday | 0.29 | 0.17 | .09 |
| Social Motives * Wednesday | 0.17 | 0.16 | .36 |
| Social Motives * Thursday | 0.34 | 0.17 | .04 |
| Social Motives * Friday | 0.38 | 0.17 | .02 |
| Social Motives * Saturday | 0.27 | 0.17 | .10 |
| Social Motives * Sunday | 0.13 | 0.16 | .45 |

Truncated Negative Binomial Regression

| Weekend Dummy Model | B | SE | p |
|--------------------------|-------|------|-------|
| Intercept | 1.07 | 0.04 | <.001 |
| Social Motives | 0.20 | 0.05 | <.001 |
| Weekend vs. Weekday | 0.38 | 0.03 | <.001 |
| Social Motives * Weekend | -0.09 | 0.04 | .02 |

| Cyclical Model | B | SE | p |
|----------------------------|-------|------|-------|
| Intercept | 1.14 | 0.04 | <.001 |
| Social Motives | 0.18 | 0.04 | <.001 |
| Amplitude (cosine) | -0.18 | 0.03 | <.001 |
| Phase (sine) | -0.20 | 0.04 | <.001 |
| Social Motives * Amplitude | 0.10 | 0.04 | <.01 |
| Social Motives * Phase | -0.01 | 0.04 | .86 |

| Full Dummy Model | B | SE | p |
|----------------------------|------|------|-------|
| Intercept | 0.61 | 0.08 | <.001 |
| Social Motives | 0.03 | 0.08 | .70 |
| Tuesday vs. Monday | 0.22 | 0.10 | .02 |
| Wednesday vs. Monday | 0.23 | 0.10 | .02 |
| Thursday vs. Monday | 0.39 | 0.09 | <.001 |
| Friday vs. Monday | 0.60 | 0.08 | <.001 |
| Saturday vs. Monday | 0.68 | 0.08 | <.001 |
| Sunday vs. Monday | 0.31 | 0.10 | <.01 |
| Social Motives * Tuesday | 0.33 | 0.10 | .001 |
| Social Motives * Wednesday | 0.12 | 0.10 | .21 |
| Social Motives * Thursday | 0.09 | 0.09 | .32 |
| Social Motives * Friday | 0.02 | 0.08 | .80 |
| Social Motives * Saturday | 0.15 | 0.08 | .08 |
| Social Motives * Sunday | 0.29 | 0.10 | <.01 |

